

Reliability of Unreinforced Masonry Bracing Walls

**Probabilistic Approach
and Optimized Target Values**

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