# Lecture Notes in Economics and Mathematical Systems

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#### 254

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### Arbitrage Pricing of Contingent Claims



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