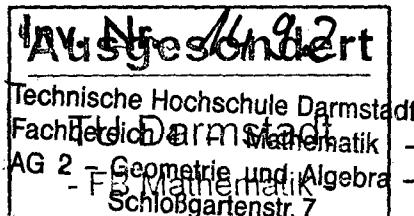


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Maple V

Language Reference Manual



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