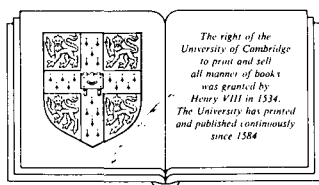


Fundamentals of nuclear physics

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CAMBRIDGE UNIVERSITY PRESS

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