
An Introduction to Econometric Theory

*Measure-Theoretic
Probability and Statistics
with Applications to Economics*

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