# Interest Rate Futures Markets and Capital Market Theory

Theoretical Concepts and Empirical Evidence

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