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Editor

# Approximation, Optimization and Mathematical Economics

With 32 Figures  
and 14 Tables



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