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# **Investment Decisions on Illiquid Assets**

A Search Theoretical Approach  
to Real Estate Liquidity

With a foreword by Prof. Dr. Heinz Rehkugler

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