

# **Statistical and Machine-Learning Data Mining**

**Techniques for Better Predictive Modeling  
and Analysis of Big Data**

**Second Edition**

**Bruce Ratner**



**CRC Press**  
Taylor & Francis Group  
Boca Raton London New York

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CRC Press is an imprint of the  
Taylor & Francis Group, an **Informa** business

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