

**An introduction to**  
**Random vibrations,**  
**spectral and**  
**wavelet analysis**

**Third edition**

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