

Tonu Puu

Mathematical Location and Land Use Theory

An Introduction

Second, Revised and Enlarged Edition
with 114 Figures



Springer

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