

Nonlinear Physical Oceanography

A Dynamical Systems Approach to the
Large Scale Ocean Circulation and
El Niño

2nd Revised and Enlarged Edition

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