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Numerical Methods in Computational Electrodynamics

Linear Systems in Practical Applications

With 173 Figures, 65 in Colour



Springer

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