



The Rational Expectations Hypothesis, Time-Varying Parameters and Adaptive Control

A Promising Combination?

by

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