Franco Nardini

Technical Progress and Economic Growth

Business Cycles and Stabilization Policies



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