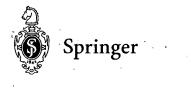
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**Editorial Committee:** 

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