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# Lecture Notes in Mathematics

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## Induced Representations and Banach \*-Algebraic Bundles

with an Appendix due to A. Douady  
and L. Dal Soglio-Hérault



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