Jean Bernard Lasserre

Linear and Integer Programming vs Linear Integration and Counting

A Duality Viewpoint

%±Springer

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