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# Learning in Economics

## Analysis and Application of Genetic Algorithms

With 52 Figures and 4 Tables

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